



5. (20points) Answer to following questions that are related to prefix sum by filling out empty box with appropriate pseudocodes.  
 (a) In prefix sum algorithm, input is a sequence of  $n$  elements  $\{x_1, x_2, \dots, x_n\}$  with a binary associative operation (binary addition) denoted by  $\oplus$ , and output is  $\{s_1, s_2, \dots, s_n\}$ , where  $s_i =$   for  $1 \leq i \leq n$ .

(b) Fill out the empty boxes in the following pseudo-code for parallel prefix sum algorithm, which is executed in parallel.

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ParallelPrefixSum ( $\langle x_1, \dots, x_n \rangle, \oplus$ )
1. if  $n=1$  then
2.    $s_1 \leftarrow x_1$ 
3. else
4.   parallel for  $i \leftarrow 1$  to  $n/2$  do
5.      $y_i \leftarrow x_{2i-1} + x_{2i}$ 
6.      $\langle z_1, \dots, z_{n/2} \rangle \leftarrow$  
7.   parallel for  $i \leftarrow 1$  to  $n$  do
8.     if  $i=1$  then  $s_1 \leftarrow x_1$ 
9.     else if  $i$  is even then 
10.    else 
11. return  $\langle s_1, \dots, s_n \rangle$ 
  
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6.(20points) Consider following C and CUDA code that adds two vectors using many-core GPU. **Write a CUDA kernel function add in the box (a) that can handle vectors with arbitrary size 'vec\_size'. Insert appropriate code into the box (b),(c),(e) for memory management, and the box (d) for CUDA kernel function call. Assume that kernel function call 'add' should generate 128 threads per block.**

<pre> #include &lt;stdio.h&gt; #include &lt;stdlib.h&gt; #define THREAD_NUM 128 // CUDA kernel 'add' should generate 128 threads per block  __global__ void add(int *a, int *b, int *c, int vec_size) { <input type="text" value="(a)"/> }  int main(void) {   int N, *a, *b, *c, *d_a, *d_b, *d_c;   printf("vector size :");   scanf("%d", &amp;N); // get the size of vectors as a user input from keyboard <input type="text" value="(b)"/>    // Alloc space for host copies of a, b, c and setup input values   a = (int *)malloc(N*sizeof(int)); vector_init(a, N);   b = (int *)malloc(N*sizeof(int)); vector_init(b, N);   c = (int *)malloc(N*sizeof(int)); <input type="text" value="(c)"/>    add <input type="text" value="(d)"/>  <input type="text" value="(e)"/>    for (int i=0; i&lt;N; i++)     printf("a[%d]=%d , b[%d]=%d, c[%d]=%d\n", i, a[i], i, b[i], i, c[i]);   free(a); free(b); free(c); cudaFree(d_a); cudaFree(d_b); cudaFree(d_c);   return 0; }   </pre>	<pre> void vector_init(int* x, int size) {   int i;   for (i=0; i&lt;size; i++) {     x[i]=i;   } }   </pre> <p><b>Example of Execution Output Result:</b>    vector size: 1234567 <input style="background-color: black; color: white;" type="text" value="&lt;--- user input"/></p> <pre> a[0]=0 , b[0]=0, c[0]=0 a[1]=1 , b[1]=1, c[1]=2 a[2]=2 , b[2]=2, c[2]=4 a[3]=3 , b[3]=3, c[3]=6 a[4]=4 , b[4]=4, c[4]=8 a[5]=5 , b[5]=5, c[5]=10 a[6]=6 , b[6]=6, c[6]=12 a[7]=7 , b[7]=7, c[7]=14 a[8]=8 , b[8]=8, c[8]=16 a[9]=9 , b[9]=9, c[9]=18 a[10]=10 , b[10]=10, c[10]=20 a[11]=11 , b[11]=11, c[11]=22 a[12]=12 , b[12]=12, c[12]=24 ... a[1234564]=1234564 , b[1234564]=1234564, c[1234564]=2469128 a[1234565]=1234565 , b[1234565]=1234565, c[1234565]=2469130 a[1234566]=1234566 , b[1234566]=1234566, c[1234566]=2469132   </pre>
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